# Focus: Solving Whole Number Addition & Subtraction Questions in Context

Nova Scotia Assessment: Mathematics Grade 3

"For learners to succeed, teachers must assess students' individual abilities and characteristics and choose appropriate and effective instructional strategies accordingly." – Helene J. Sherman

# LESSON LEARNED estions in Context



# **Purpose of this Document**

This Lessons Learned document was developed based on an analysis of the Item Description Reports for the Nova Scotia Assessment: Mathematics in Grade 3 (NSA-M3). This document is intended to support all classroom teachers at grades Primary – 3, and administrators at the school, region, and provincial levels. The focus of the document is to help educators work through the process of taking in the information provided by the data analysis and see how it can inform lesson design and assessment in the classroom.

It is suggested that school teams make use of this resource in concert with their school's Item Description Report provided by the Department of Education and Early Childhood Development to all regional centres for education. These reports include student achievement data at the school, regional centre, and provincial level for all questions appearing on the Mathematics in Grade 3 Assessment. By analyzing their own performance on groupings of questions dealing with similar outcomes, schools can identify areas of strength and areas where changes in instruction and/or assessment might be made. This process is designed to foster continued discussions, explorations, and support for mathematics focus at the classroom, school, regional centre, and provincial levels that are all based on valid and reliable data.

This document specifically addresses some of the areas that students across the province found challenging based on provincial assessment data. It is essential that teachers consider assessment evidence from a variety of sources to inform the next steps most appropriate for their students. Effective classroom instruction and assessment strategies are responsive to the individual learners within a classroom.

This document highlights those outcomes where students seem to require additional support. It provides some information about student performance on the assessment in addition to suggested classroom instruction strategies. Sample assessment items are included for each topic explored.

### **Overview of the Nova Scotia Assessment: Mathematics in Grade 3**

Nova Scotia Assessments are large-scale assessments that provide reliable data about how well all students in the province are learning the mathematics curricula. It is different from many standardized tests in that all questions are written by Nova Scotia teachers to align with curriculum outcomes and the results reflect a snapshot of how well students are learning these outcomes. These results can be counted on to provide a good picture of how well students are learning curriculum outcomes within schools, regions and in the province. Since the assessments are based on the Nova Scotia curriculum, and are developed by Nova Scotia teachers, results can be used to determine whether the curriculum, approaches to teaching and allocation of resources are effective. Furthermore, because individual student results are available, these, in conjunction with other classroom assessment evidence, help classroom teachers understand what each student has under control and identify next steps to inform instruction.

The assessment provides information about mathematics for each student and complements assessment data collected in the classroom. This assessment is administered at the end of Grade 3. It is designed to provide detailed information for every student in the province regarding their progress in achieving a selection of mathematics curriculum outcomes at the end of Grade 3. Information from this assessment can be used by teachers to inform their instruction and next steps in providing support and intervention for their students.

# **Lessons Learned Overview**

Provincial assessments and examinations generate information that teachers can use to help inform classroom instruction and assessment. Following the analysis of each assessment or examination, patterns and trends are identified. These include areas of strength and areas for growth. The Lessons Learned documents specifically highlight concepts where growth is still needed.

There are four areas that have been identified as the areas of focus for this Lessons Learned document. They are:

- Solving whole number addition and subtraction questions in context.
- Measuring and estimating length.
- Identifying and sorting irregular polygons.
- Interpreting data represented in tables and graphs.

*This section specifically addresses solving whole number addition and subtraction questions in context*. It begins with an overview of the student errors and misconceptions identified through the provincial assessment. These include:

- Place Value
- Number and word grabbing in story problems
- Use of different representations

Strategies are then outlined that are designed to enhance student comprehension, drawing from researched best practices. The strategies emphasize the integration of essential models, tools, and interconnections to facilitate the transition between concrete, pictorial, and abstract representations of concepts, highlighted by the importance of deliberate planning and purposeful questioning. To support both assessment and instruction, sample lesson activities are presented alongside a series of cognitive-level questions, providing educators with ideas for addressing knowledge gaps and fostering strategic reasoning and problem-solving skills. Each section culminates with a selection of print and online resources, as well as recommended manipulatives to support professional learning and student understanding of that topic.

### Solving Whole Number Addition and Subtraction Questions in Context

Alignment to previous Outcomes			
<b>PN04:</b> Students will be expected to represent and describe numbers 2 to 10 in two parts, concretely and pictorially.	<b>1N09:</b> Students will be expected to demonstrate an understanding of the addition of two one-digit numbers and the corresponding subtraction, concretely, pictorially, and symbolically, in join, separate, and part-part-whole situations.	<b>2N09:</b> Students will be expected to demonstrate an understanding of addition (limited to 1- and 2-digit numerals) with answers to 100 and the corresponding subtraction.	

#### What conclusions can be drawn from the NSA: Mathematics in Grade 3?

Students understand addition and subtraction of whole numbers with answers up to 1000, however some have difficulty when there is a need for regrouping. In questions where students were explicitly given all the information needed to do a knowledge question, students were successful. Yet, when given application and analysis items, that required higher order thinking skills when problem solving only half of the students were successful. This is evident in contextual problems within the assessment.

Students did well when translating and moving flexibly between and among representations of a concept. However, when presented with non-conventional formats, some students struggled. Therefore, students should be encouraged to use multiple representations to continue to be able to translate between words, pictures, or symbols. This includes, for example, various representations of numbers. When students are working to partition whole numbers and to perform operations, it is very important for students to understand that numbers can be broken down into two or more parts in many ways. This supports how students work with numbers and apply varying strategies when problem solving. Overall, helping them build their toolbox of strategies to solve contextual problems and further develop their reasoning abilities.

#### **Related Outcome**

**3N09:** Students will be expected to demonstrate an understanding of addition and subtraction of numbers (limited to 1-, 2-, and 3-digit numerals) with answers to 1000.

#### Why is this an area of need and how can we support students?

	Place Value	
Misconceptions/Errors in Student Work	Possible Next Ste	ps in the Classroom
When students are asked to solve addition or subtraction questions, you may get the following responses.	Each of the different type of responses provides clues as to the root of the misconception. Be understand what the student understands well and tailoring their learning from their starting	
Sample question.	Regardless of what the student understands, using various forms of rep their thinking.	presentation can only f
What is 573 – 245?	lising and Modelling with a Number Line	
A. 322 (student subtracts with trading in tens position, but still subtracts incorrectly in ones position)	Use an open number line to solve for addition and subtraction. More so, students focus on breaking numbers into friendlier chunks that	del and encourage co support flexibility, ef
B. 328 (correct answer)	5 40 100 100	
C. 332 (student subtracts smaller digits from larger digits)	Image: state	
D. 338 (student subtracts with trading – ones position, but forgets when subtracting in tens position)	573 - 100 = 473 473 - 100 = 373 373 - 40 = 333 333 - 5 = 328	
Sample question.	Modelling with Base 10 Material	Recording Place
What is 179 + 22?	To help students focus on the place value rather than the digits, model and practice using base-ten blocks	The traditional alg Have students bre
A. 191 (student forgets to add in the ten when determining the sum the digits in the tens position)	identify how the strategies are similar.	179 + 22
B. 201 (correct answer)	Hundreds Tens Ones	179 is the same as
C. 291 (student adds ten tens rather than one ten when determining the sum of the digits in the tens position)		So,
D. 1911 (student does not regroup)		100 + 70 + 9 <u>+ + 20 + 2</u> 100 + 90 + 11
		100 + 90 = 190

efore planning next steps, it is important to goint.

further their understanding and or add flexibility to

ounting up and counting back as strategies. In doing fficiency, and accuracy.

#### Value

gorithm focuses on digits rather than place value. Teak numbers into their place value and have them on and subtraction.

as 100 + 70 + 9 s 20 + 2

190 + 10 + 1 = 201 (Answer)

While not an error or a misconception perse, one could also infer that students may not be checking for reasonableness in their answers. They could be stuck in incorrectly using standard procedures negating what they know about number sense. Students may also not be aware of other, more helpful strategies that support how to work with numbers to solve what is unknown in a story problem.

For example, when students respond with an answer of 291 to the question above (179 + 22), they may not be thinking that the number should be close to 200 based on the size of both numbers. They could be more caught up in using a procedure and not in the practice of checking for reasonability.

#### To solve 179 + 22

(Hundreds) 100 (Tens) 70 + 20 = 90(Ones)  $9 + 2 = 11 \rightarrow 10 + 1$ (Tens) + (Ones) (Answer) 100 + 90 + 10 + 1 = 201

#### **Estimation strategies**

Students need to be encouraged to estimate before calculating an answer to a question. Estimating sums and differences is valuable as it helps in checking the reasonableness of calculations, and predicting answers, and sometimes it is all that is required. The goal of estimation is not to get the exact answer but to get a close approximation quickly and efficiently. It is a valuable skill for mental math and for quickly checking the reasonableness of answers.

To estimate sums and differences, students might use strategies that include rounding to a multiple of 10, 100, or 1000, rounding one number and not the other, front-end estimation, and rounding one number up and the other down. Students may also choose friendly or benchmark numbers that are easier to work with and are near the given numbers. Further examples can be found in the guides. At the core of estimating is understanding number relationships, benchmark numbers, and compatible numbers.

#### Number Talks

Number talks foster the development of number sense by encouraging students to think flexibly about numbers and mathematical operations. Through engaging in discussions and exploring various strategies, students deepen their understanding of mathematical concepts. Moreover, number talks promote mathematical discourse, as students articulate their reasoning, listen to their peers' strategies, and engage in collaborative problem-solving. Hence, number talks support the use of multiple strategies for problem-solving, reinforcing the idea that there are often multiple paths to a solution. They also facilitate the development of mental math skills by providing opportunities for regular practice. Furthermore, number talks can be adapted to meet the needs of diverse learners, making them a versatile tool for differentiated instruction. They offer valuable insights into students' mathematical understanding, enabling teachers to assess student progress and plan future instruction accordingly.

#### **Retrieval Practice Strategies**

It is essential that students know their addition and subtraction facts and understand how numbers relate to each other. Retrieval practice supports instruction and assessment by strengthening schemas that students have built, helping them commit the information to their long-term memory. Retrieval practice involves daily cumulative review and improves the efficiency of learning. Examples include making and using flashcards, concept maps, or grids, intentional games, choral response, and interleaved practice. All of which facilitate better learning than highlighting or re-reading questions.

#### **Activities to Support Lesson Planning**

#### Number Talk and Number Strings

Use number talk routines to develop efficiency, flexibility, and accuracy with computations. They help to elicit specific strategies that focus on number relations and number theory rather than a series of steps found in traditional algorithms. Classroom conversations and discussions around purposefully crafted computation problems are at the very core of number talks.

A few examples are outlined below, while further examples of strategies are outlined in the curriculum guides as well as the resources section.

Using manipulatives like counters, Cuisenaire rods, and open number lines support how students visualize counting and quantity along with adding and subtracting.

Begin with examples that require less cognitive load to support the development of effective strategies and models. These can include activities that focus on number relationships, compatible numbers, and benchmark numbers. Encourage flexibility and talk about estimation.

#### Grade P

Goal - recognizing different ways to make the value 5.

Briefly show students one of the arrangement of dots. Discuss using one or more of the question prompts below. Then show the second image and then the third, discussing in between. Can students identify 5 in different ways?



#### **Question prompts:**

Knowledge: How many dots do you see? How do you see them?

Application: How does your strategy compare to the strategies shared by others in your group?

Analysis: Create your own arrangement and show me how you determined how many dots. How does it compare to the ones we discussed as a group? (Note: this question can be used after the discussion to check for individual understanding.)

OR

Grade 1
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Goal – making and relating to tens using ten frames.

Show students one of the pairs of dots in the ten frames. Discuss using one or more of the question prompts below. Show the second pair and then the third, discussing in between.



#### **Question prompts:**

Knowledge: How many dots do you see? How do you see them?

Application: How does your strategy compare to the strategies shared on the board?

Analysis: Create your own arrangement and show me how you determined how many dots. How does it compare to the ones we discussed as a group?

(Note: this question can be used after the discussion to check for individual understanding.)

OR

<b>Goal</b> – break each number into its Place Value.
You can select either the addition or the
subtraction. Show each number sentence one at
a time and have students solve it; discussing in
between. What common strategies are students
using and are they seeing the relationship
between the values?

Grade 2

18 + 31	20–10
23 + 14	20–9
37 + 12	<b>20 – 1</b> 1
32 + 25	21–9

#### **Question Prompts:**

Knowledge: Solve the number sentence. Explain your strategy or state your strategy.

Application: How are these strategies the same? How does the previous number sentence help you solve this number sentence?

Analysis: Create your own number sentence that relates to these number sentences and would use the same or similar strategy.

OR

#### Grade 3

**Goal** – breaking each number into its Place Value

You can select either the addition or the subtraction. Show each number sentence one at a time and have students solve it; discussing in between. What common strategies are students using and are they seeing the relationship between the values?

35 + 19	59 – 47
115 + 92	60 – 50
167 + 73	60 – 47
115 + 193	62 – 45

#### **Question Prompts:**

Knowledge: Solve the number sentence. Explain your strategy or state your strategy.

Application: How are these strategies the same? How does the previous number sentence help you solve this number sentence?

Analysis: Create your own number sentence that relates to these number sentences and would use the same or similar strategy.

#### OR

Show students the following arrangement of Cuisenaire rods.



Ask students:

Knowledge: What do you notice? What do you wonder?

Application: Investigate a wonder question. For example, how many whites make a green? How many reds make a purple? Have students build representations of their thinking.

Analysis: How many different ways can you show the same length as the yellow?

Show students the following arrangement of Cuisenaire rods. You may need to have students build the 'staircase' depending on how familiar they are with the tool.

Ask students:

Knowledge: Which rod is the same length as these two rods?

Next show the following arrangement:

Knowledge: Which rod(s) is the same length as these two rods?

Application: How did the first arrangement help you answer the second arrangement?

Next show students the following arrangement:

Knowledge: Which rod(s) is the same length as these two rods?

Application: How did the first two arrangement help you answer the second arrangement? What other rods can be used that would be the same length as these two rods?

Analysis: Create your own length(s) and show me how you determined what other rod(s) matched the length. How does it compare to the ones we discussed as a group? What strategies help you know what lengths are easier or more difficult to compare?

Note: Some grade 2 students may start here to support readiness of breaking numbers in friendly or benchmark amounts when adding. A similar arrangement using smaller numbers can Instead of showing students the number sentences above, use an arrangement of coins or ten frames to show addition and/or subtraction. The coins (addition) and ten frames (subtraction) below represent the number sentences listed above.

The same prompting questions above, can be used with visual representations to support student thinking.

Addition:



1¢

5¢ 10¢ 10¢

Subtraction:

20 - 10













20 - 9

To help students visualize benchmark values and place value, use base ten blocks as a visual representation. Students can physically make groups of ten to transition into making groups of ten mentally. Some students may visualize and manipulate the materials in their head.

The same prompting questions can be used with visual representations to support student thinking. Here are a couple of examples for both addition and subtraction.







#### Number and Word Grabbing in Story Problems

#### **Possible Next Steps in the Classroom**

Students use learned strategies to look for numbers and key words in a story problem and use these to create a number sentence. In doing so, they add or subtract using the two numbers without understanding the action taking place in the problem and checking if their solution is reasonable.

**Misconceptions/Errors in Student Work** 

Students may:

- overgeneralize all stories to addition.
- not see part-part-whole relationships.
- subtract a whole from a part.
- not understand the relationship between addition and subtraction.

#### Here are two examples of story problems and possible student answers.

The first is a Separate Problem: Result Unknown.

#### Stacey went to the store and spent \$18.

- If Stacey had \$50 to begin with, how much money is left?
- \$32 (correct answer)
- \$42 (an error that occurs when a student incorrectly borrows and subtracts in the tens place)
- \$48 (an error that occurs from a student that subtracts the smaller digits from the larger digits)
- \$68 (an error that occurs when a student adds as opposed to subtracts)

This second is a Join Problem: Change Unknown.

Stacey had \$18 saved in a piggy bank at home. After mowing 3 lawns in the neighbourhood, Stacey now has \$50.

How much money did she earn for moving the lawns?

- \$32 (correct answer)
- \$42 (an error that occurs when a student incorrectly borrows and subtracts in the tens place)
- \$48 (an error that occurs from a student that subtracts the smaller digits from the larger digits)
- \$68 (an error that occurs when a student adds as opposed to subtracts)

# Developing an understanding of the relationship between addition and subtraction

In addition to strategies listed in the previous section, adding and subtracting must also be explored in meaningful contexts using a variety of concrete materials and pictures to model and compare contexts. Math tools and models like: Rekenreks, ten frame, linking cubes, number lines, base-ten blocks, Cuisenaire rods, and strip diagrams are helpful at visualizing quantity and developing personal strategies. When teaching both concepts, spend time on addition and subtraction separately, but also together to help students develop the understanding of how adding and subtracting are opposites of one another and how each is presented in questions.

#### **Developing parts-whole relations**

Model joining and separating problems using part-part whole mats (Strip Diagrams) and encourage students to do the same to help interpret story problems. Students must also experience addition and subtraction in comparison situations. They need to learn that addition and subtraction problems can be categorized based on the kinds of relationships they represent.

Join Problems	Separate Problems	Part-Part- Whole Problems	Compare Problems
Result U	Inknown	Whole Unknown	Difference Unknown
Change l	Jnknown	Part Unknown	Larger Unknown
Initial U	nknown		Smaller Unknown

Further details can be found in the curriculum guides.

#### **Teaching About and Through Problem Solving**

Provide direct instruction on problem-solving strategies as students share their own solutions and findings. Use students' methods to guide instruction. Elaborate on the methods used by students to solve and justify and encourage students to comment and ask questions of their peers.

Concepts and skills should be connected to everyday situations and other curricular areas. Encourage students to make connections to make mathematics come alive through math-to-world, math-to-math, and math-to-self connections.

Develop students' mathematical vocabulary, initiate effective ways to navigate informational text, and encourage students to reflect on what they have learned.

Embed strategies/tools such as the Frayer Model, Concept Circles, and Exit Cards to assess student learning.

#### Modelling Thinking with Think Alouds

A teacher should model problem solving with students by sharing aloud their thinking as they read to understand a problem. Through the process, students learn how to verbalize to understand a question and to make sense of what is being asked and what is in their toolbox to answer the question.



#### Activities to Support Lesson Planning

#### **Open Tasks**

Using open tasks and games offers ways for students to apply and demonstrate addition and subtraction in context and allow for multiple entry points. Cross-strand opportunities also help to reinforce and help students to see mathematics as holistic and not siloed into its strands. They can also be used across multiple grades and abilities. Games that include dice and cards also encourage students to determine count and quantity, and sums and differences of numbers in a fun and interactive way.

The following activities can be set up to support a problem-solving lesson. Using common literacy strategies that help students make sense of different types of texts can also be used to support understanding a story problem. This includes think-alouds to model and engage in conversation with students.

Grade P	Grade 1	Grade 2	
Using dot plates or counters in small groups, pairs	Students can physically move around the room or	Have students use manipulatives like Cuisenaire	ŀ
or individually.	use counters or Cuisenaire rods to work through the	rods, open number lines, base ten blocks, and strip	r
	various questions.	diagrams to show their thinking.	С
Have two groups of counters or dot plates (e.g., one			
with 3 dots and one with 4 dots).	Knowledge: How many students in the class have	Knowledge: If there are 76 students with blue eyes	k
	brown eyes? How many have blue eyes? How many	and 47 students with brown eyes, how many all	а
Knowledge: Show both groups and ask how many	all together.	together? What is the difference in the number of	t
altogether. Watch how the student combines the		students?	S
count.	Application: How many more students have		
	brown/blue eyes?	Application: If there are 38 students in grade 2 and	A
Application: Which group has more? How do you		almost 20 students have blue eyes, how many have	а
know?	Analysis: If 4 new students joined the class, how	brown eyes?	ł
	many students would have blue eyes and brown		
Analysis: How can you arrange the dots/counters to	eyes, now. What would be the new totals, and	Analysis: Create and solve number sentences. How	A
help you know how many and how much more	which one would be greater and by how much?	many students have blue eyes and how many have	r
without counting?		brown eyes? What is the sum? What is the	b
		different?	С

#### Grade 3

Have students use manipulatives like Cuisenaire rods, open number lines, base ten blocks, and strip diagrams to show their thinking.

Knowledge: If there are 176 students with blue eyes and 217 students with brown eyes, how many all together? What is the difference in the number of students?

Application: If there are 386 students in the school and almost 150 students have blue eyes, how many nave brown eyes?

Analysis: Create and solve number sentences. How many students have blue eyes and how many have prown eyes? What is the sum? What is the different?

#### Misconceptions/Errors in Student Work

If asked to interpret or represent a question where representation varies, some students have difficulty translating between pictures, words, or symbols.

Students should recognize the various representations they can use when solving a number problem.

Examples:

Students need to demonstrate their knowledge of place value pictorially using non-conventional representations.

Choose the number represented by the base-ten blocks.



- 11 (total number of blocks and not the value they represent)
- 326 (correct answer)
- 623 (a student has switched the values of the unit cubes with the flats)
- 14312 (reading the number of blocks from right to left, with no regard for place value)

Students need to demonstrate their knowledge of place value in words using non-conventional representations.

The number 642 is the same as:

- 5 hundreds, 2 tens, and 14 ones (regroups 14 ones incorrectly as 1 hundred and 4 tens)
- 64 tens and 2 ones (correct answer)
- 6 tens and 42 ones (reads 6 tens as 6 hundred but correctly identifies 42 ones)
- 6 hundreds, 20 tens, and 4 ones (misidentifies tens and ones place values)

#### Use of Different Representations

#### Possible Next Steps in the Classroom

#### Engage in dialogue and encourage purposeful selection of representations

One way to encourage students to use multiple representations is to explicitly ask for them. Engage in dialogue about the explicit connections between representations and alternate between them. Encourage students to purposefully select various representations to check for understanding. Discuss a variety of reasons to use a particular representation, including but not limited to efficiency, accuracy, ease of use, appropriateness with the problem context, and student preference. By comparing and discussing the use of multiple representations for the same problem, students can more easily see the suitability of one representation over another.

For example, representing a story problem with a strip diagram or using base-ten blocks or an open number path / number line to model addition and subtraction. Equality can be represented in both an equation, but also visually using a balance scale.

When working with story problems, help students to identify whether the problem is joining, separating or part whole. This will help in how students use strip diagrams to identify what is given and what has to be determined.

For example, the question Bobby had 98 stamps. Bobby was given more by a friend. Now Bobby has 137 stamps. How many stamps did Bobby get from the friend.

98	?
	137

This is represented by an equation as follows: 98 + \_\_\_ = 137 but can then be solved using different strategies that may include subtraction or adding up.

Other models include the examples below:

Base-ten blocks

Number Path



30 – 6 =







When students are more commonly presented with one version of a story problem, i.e. result unknown, they will typically misuse a strip diagram. See example:

Bobby had 98 stamps. Bobby was given more by a friend. Now Bobby has 137 stamps. How many stamps did Bobby get from the friend.

?	
98	137



It is also important to present to students with non-conventional displays of whole numbers to support thinking and reasoning. These include base ten blocks and expanded notation.

#### Concrete Representational Abstract (CRA) Modeling

This approach is a system of learning that uses physical and visual tools and models to build students' understanding of abstract concepts.

Students are introduced to a new mathematical concept using concrete resources (e.g. base-ten blocks, ten-frames). When they are comfortable solving problems with physical aids, they are given problems with pictures – usually visual representations of the concrete objects they were using.

Then students are asked to solve problems where they only have the abstract, i.e. numbers or other symbols. Building these steps across a lesson can help students better understand the relationship between numbers and the real world, and therefore helps secure their understanding of the mathematical concept they are learning.

It is important to note that learning takes time and students should not be rushed into using abstract representations. Students should be using tools and representations everyday to support and check for understanding.

#### Activities to Support Lesson Planning

When designing instruction, use activities that encourage the use of tools and different representations that align to the development of the mathematical concept.

Games that utilize math manipulatives are a great way to integrate the use of various representations to build number sense and reinforce skills, while engaging students in the learning process. These should be intentional and target and reinforce skills and concept development.

Grade P	Grade 1	Grade 2	
Knowledge: Using a Rekenrek or counters, have students represent a number of their choice. How do they know they are correct? Application: How many ways can you show the number 5 using a Rekenrek or counters? How many of one colour and how many of the other do you use to show 5? How do you know they are the same? What number can you make using these two groups of cubes? (e.g., 3 red cubes and 2 green cubes make how many cubes all together) Analysis: How can you arrange your counters to help you see the number 5 without counting? How does it help you?	Knowledge: Have students model a group of 3 then have them model a group of 4. Ask, how many items are there altogether? Application: Hide 3 small items in your hand or under a piece of paper. Tell students that 3 items are hidden. Put out 4 more items where students can see them. Give students additional counters to model the 3 hidden items if they need them. How many items are there altogether? Analysis: How many more items are there in this group than the hidden one? You can also use the two colours on a Rekenrek to help students to notice different ways of making different numbers up to 10 or 20.	Grade 2Knowledge: Using base-ten materials, show the following in different ways. Represent each value in different ways. $45 + 28 =$ $45 - 12 =$ Application: Using base-ten materials, show all possible sums and differences using these values: 12, 28, 45. Are there calculations you found more challenging? Easier? Are there other ways you can represent the given numbers to help you solve the problems?Analysis: Ask students to determine which numbers are missing. Hint: all rows, columns, and diagonals add to the same amount. $\boxed{17$ $22$ $19$ $\boxed{19}$ $23$ $20$ $25$ $\boxed{19}$ *To create additional magic squares, you can always begin with one that you have, like the one above, and add, subtract, multiply, or divide all entries using the same value. You can also rotate or reflect the square. Have students create their own.	K fc d A p8 c rc p A a a a a a a a a a a a a b a a a b a a a b a a a b a a a b a a b a a b
			0

#### Grade 3

nowledge: Using base-ten materials, show the ollowing in different ways. Represent each value in lifferent ways.

128 + 82 = 145 - 82 =

application: Using base-ten materials, show all possible sums and differences using these values: 2, 128, 145. Are there calculations you found more challenging? Easier? Are there other ways you can epresent the given numbers to help you solve the problems?

nalysis: Ask students to determine which numbers re missing. Hint: all rows, columns, and diagonals add to the same amount.

	51	66
57		69
60	75	

21	51	66
57	12	69
60	75	3

\*To create additional magic squares, you can always begin with one that you have, like the one above, and add, subtract, multiply, or divide all entries using the same value. You can also rotate or reflect the square. Have students create their own.

# What are some sample questions to help support assessment?

Cognitive Level	Grade P	Grade 1	Grade 2
Knowledge	How many counters altogether?	How many dots are there altogether?	What number is represented by the base-ten blocks?
	What number comes next as I count3, 4, 5,	How many blocks am I taking away? What is left?	46 + 36 = 46 + = 82 88 - 36 = 48 = + 24
			Write an expression that can be used to represent 53. Using an open number line, determine the sur of 23 and 36.
		Write addition fact families that contain 5 as one of the numbers.	Using an open number line, determine the difference between 78 and 46.

#### Grade 3

What number is represented by the base-ten blocks?
Write two different expressions that can be used to represent the 597.
127 - 38 = 326 + 48 = 48 + = 326 127 = + 38
What two numbers could you add to get a sum of 123?
What two numbers could you subtract to get a difference of 56?

#### Application

# Fill in the number that come before and after the following numbers.



You have 4 crayons, and your friend has 4 crayons. How many crayons do you have altogether?

Represent the number 5 in different ways?

What number sentence do these dots represent?



What number sentence do these base ten blocks show?



You have 8 cubes. There are 5 red cubes, and the rest are green. How many cubes are green?

Do you think the sum of 5 + 9 will be larger or smaller than 15? Explain.

What equation is represented by the strip diagram?

42
26

What equation is represented by the number line shown?



I made 43 cookies and gave 21 away to my classmates. How many cookies do I have left?

My friend has a book with 48 stickers, and I have a book with 32 stickers. How many more stickers does my friend have?

Do you think the sum of 34 + 57 will be larger or smaller than 100? Explain.

Which addition problem is represented by this set of base-ten blocks?

When travelling to our vacation spot, we drove 239 km and stopped for lunch. How much further do we have to drive if the total distance to our destination is 526 km?

Create a strip diagram to model the following situation: You are saving money to buy a new bike. You are given \$65 for your birthday and now you have \$126. How much money did you start with?

Do you think the sum of 134 + 458 will be larger or smaller than 600? Explain.

Analysis	Represent the counters shown in two parts.	Create your own story problem using the following numbers: 6, 7, 13.	The answer is 94, what is the question?
	Part Part	How are these number sentences the same and how are they different?	Create your own story problem using the following numbers: 16, 47, 63.
		6+5=11 11-5=6 11=5+6 5=11-6	I made 43 cookies. Some are oatmeal cookies, and some are chocolate chip cookies. How many of each cookie did I make?
	You have 8 cubes. Some are green and some are red. How many of each do you have?	You have 10 apples and eat 2 of them each day. What day will you have zero apples?	I gave some cookies away to my friends. If I made 43 cookies and only had 12 left, how many cookies did I give away?
	You have 8 cubes. There are 5 red cubes, and the rest are green. How many cubes are green?	You have 8 cubes. Some are green and some are red. How many of each do you have?	Is 84 close to 0, 50, 80, 90, or 100? How do you know what number it is close to?
	Is 4 close to 0, 5, or 10? How do you know what number it is close to?	Is 14 close to 0, 10, 15, or 20? How do you know what number it is close to?	

You have been given a handful of money. You notice you have a mixture of nickels, dimes, and quarters. You decide to use the money to buy a used book for 85 cents. If you use all the money to buy this book, how many nickels, dimes and quarters did you have? What do you notice about the types of coins you are using?

Pete has 123 cards and gives some to his friend. Now Pete has 86 cards. How many more cards does Pete have than his friend?

Each shape represents a different number. Find a number that each shape could represent. Select one or more to solve.

+ 📕 + 🔵	= 39
+ • +	+ 📥 = 36
+ • + 🔺	= 27

Is 184 close to 100, 150, 180, 190, or 200? How do you know what number it is close to?

# Supporting Resources

# Manipulatives and Models to Support Learning

Counters	Linking cubes	Rekenreks	Ten frames	Base-ten blocks
Number path (P-1)	Cuisenaire Rods	Balance Scales	Strip Diagrams	Dominoes
1 2 3 4 5 6 7 8 9 10   Open Number line (2-3)			Equation: =	



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